

# **BPS K-12 Math Program Overview**

May 17, 2016

# Focal Points

## **District-Wide Strategic Objectives**

**Coherent, Higher Order Thinking and  
Student-Centered Learning**

**Equity and Diversity: Teaching all Students**

**Collaborative Professional Culture**

# **K-5 Mathematics**

Aligned to 2011  
Massachusetts Math Standards  
Common Core

# K-5 Coherent, Higher-Order Thinking, Student-Centered

## DAVIS K-2

Bridges in Mathematics, 2nd Edition

Comprehensive : Two components: Number Corner and Units (lessons and workplaces)

Whole group and small group work instruction

Approximately one hour per day

Transition to Lane School

## LANE SCHOOL 3-5

EnVision 2012 - Common Core Edition

Comprehensive: 16 Topics + Performance Tasks

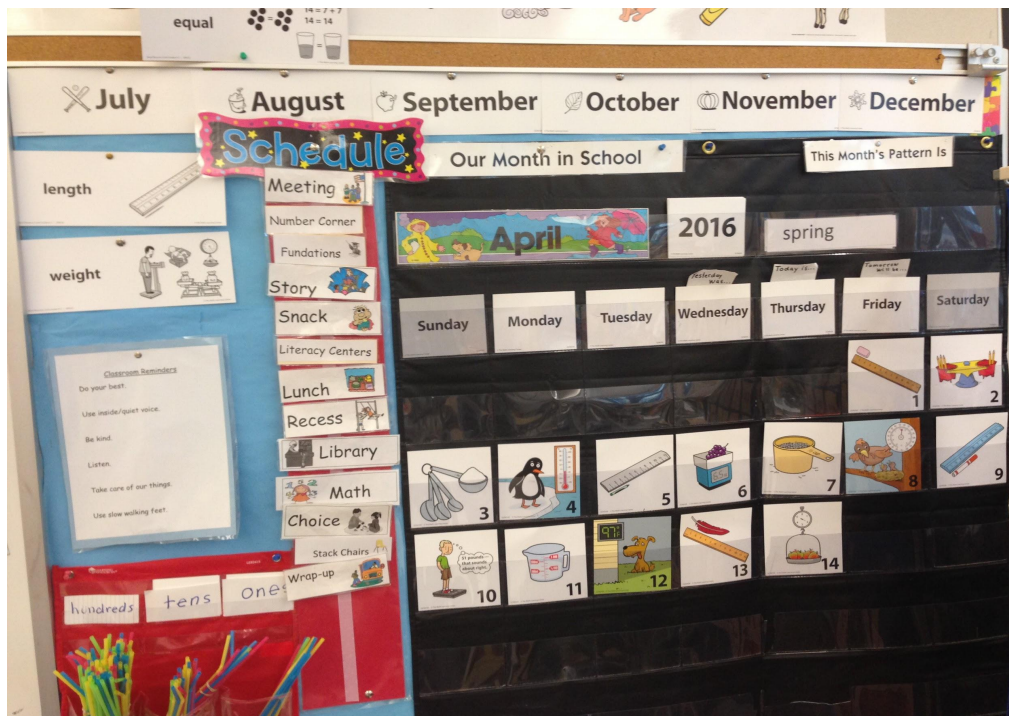
Extremely well-scaffolded

Approximately one hour per day

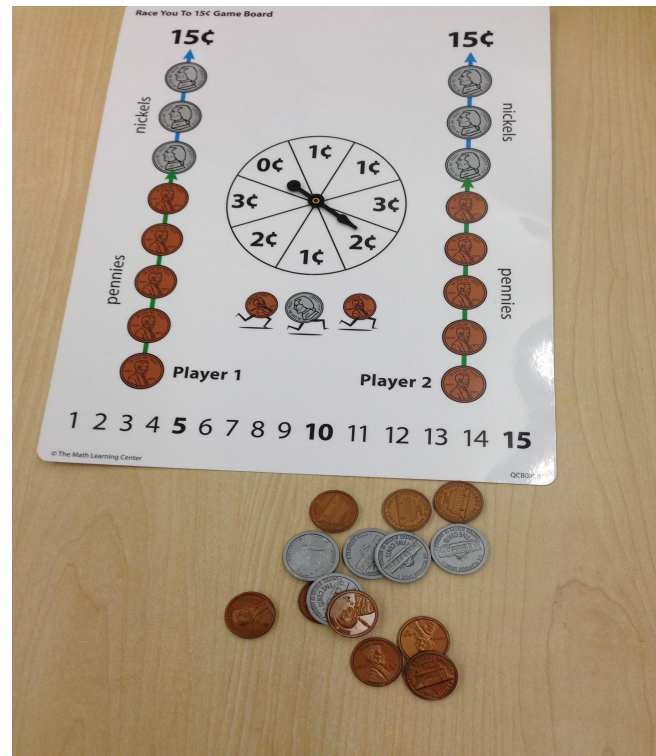
Transition to JGMS

# Davis Number Corner and Workplace Examples

## April Calendar - Kindergarten Classroom



## Kindergarten Money Game



# Davis Higher-Order Thinking Skills

*“ I think one of the strengths of the program clearly includes a focus on getting children to “think” like a mathematician and to practice the set of Mathematical Practices that are outlined in the Common Core State Standards. There are many examples of how to get children to articulate their understandings and strategies.”*

**Davis School Kindergarten Teacher**

*“ The Bridges developers have done a beautiful job balancing the research on the best math practices while keeping in mind the developmental ages/stages of six- and seven-year old learners. The materials are truly multi-sensory: white boards, number racks, number lines, many manipulatives like pattern blocks, Unifix cubes, and counters...The games are engaging for the children. The students are having fun with frogs and flies chasing each other on the number line, performing word problems with their number racks, and practicing math facts with card and spinner games. The children work in partnerships, work by themselves and with the teacher. It’s all there.”*

**Davis School Grade One Teacher**

# Davis Higher-Order Thinking Skills

Solve each story problem below. Use numbers, pictures, or words to help solve the problem and show your thinking. Write your answer on the line.

- a** Sam has 5 apples. Ella has 9 apples. How many more apples does Ella have than Sam?



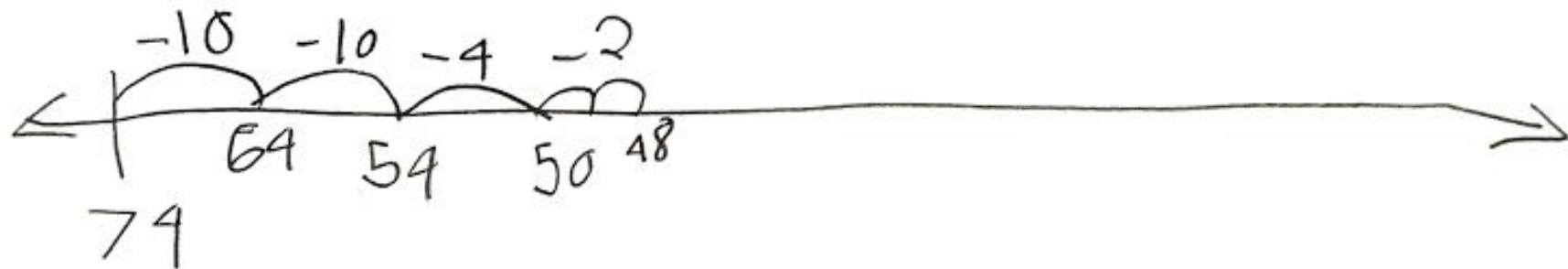
Grade one  
Story problems

Ella has 4 more apples than Sam.

# Davis Higher-Order Thinking Skills

$$74 - 26 = 48$$

Grade 2  
Double-digit subtraction





# Collaborative Problem-Solving



# Lane School: Grade 4 Task

The perimeter of a state park shown is 42 miles.



4th Grade  
Performance Task

A ranger estimates that there are 9 deer in each square mile of the park.

If this estimate is correct, how many total deer are in the park? Explain your answer using numbers, symbols and words.

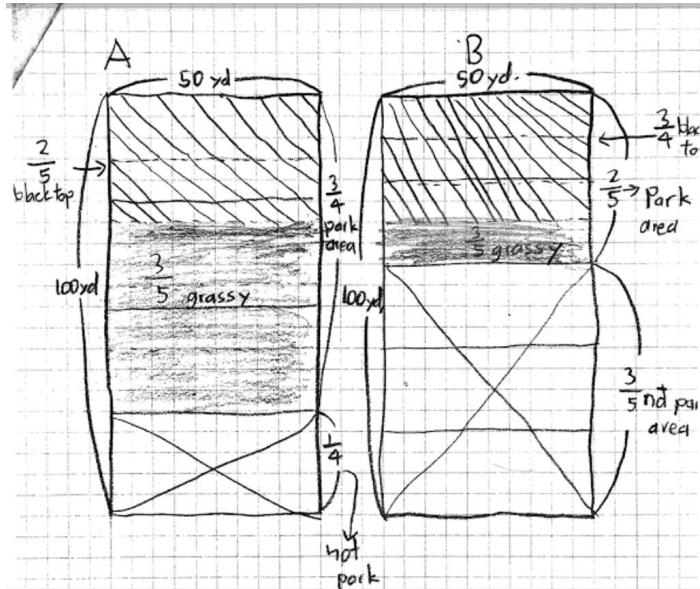
Student solution (verbatim): (Just typed for ease of reading)

If the ranger's estimate was correct, there would be 936 deer in the state park. We know this because since 42 is the perimeter, and the shape of the park is a rectangle and one side is 8 miles, then the two short sides measure  $8 \times 2 = 16$ . Then we know that  $42 - 16 = 26$ , so 26 is the perimeter of the two long sides.  $26 \div 2 = 13$  so 13 miles is the length of one of the two other sides. Then, to find the area, we did  $13 \times 8 = 104$  sq. miles ( $A = l \times w$ ). The ranger from the park estimated there were 9 deer per square miles, so we multiplied  $9 \times 104 = 936$ . 936 is the amount of deer in the state park if the ranger is correct.

Two communities, A and B, have parcels of land that measure 50 yards by 100 yards. In community A, they have been asked to convert  $\frac{3}{4}$  of their lot to a playground, and  $\frac{2}{5}$  of that playground should be covered with blacktop. In community B, they are building their playground on  $\frac{2}{5}$  of the lot, and  $\frac{3}{4}$  of the playground should be blacktop.

## Lane School: Grade 5 Task

In which park is the grassy playground bigger? In which lot is the blacktop bigger? Illustrate and explain your answers.



A.

$$5000 \text{ yd}^2$$

$$\downarrow$$

$$\frac{3}{4} \text{ is } \frac{3}{4} \times \frac{1250}{1} = 3750 \text{ yd}^2$$

$$\downarrow$$

playground space

$$\frac{3750}{1} \times \frac{2}{5} = 1500 \text{ yd}^2$$

$$\downarrow$$

blacktop

$$\frac{3750}{1} \times \frac{2}{5} = 1500 \text{ yd}^2$$

$$\downarrow$$

grass

B.

$$5000 \text{ yd}^2$$

$$\downarrow$$

$$\frac{5000}{1} \times \frac{2}{5} = 2000 \text{ yd}^2$$

$$\downarrow$$

playground space

$$\frac{2000}{1} \times \frac{3}{4} = 1500 \text{ yd}^2$$

$$\downarrow$$

for black top

$$2000 - 1500 = 500 \text{ yd}^2 \rightarrow \text{grass}$$

$> \frac{2}{5}$  D. Park A has more grassy area than Park B.  
 $\frac{2}{5} = \frac{2}{5} \times 320 = 128$ . The (A/B) both have the same amount of space for blacktop.

# K-5 Equity and Diversity: Teaching All Students

All (but a few) students receive the core curriculum and common assessments at grade level.

**Heterogenous** classes until Fifth grade: Flexible Grouping model in 5th

**Remedial support:** In class or pull-out with Special Educators and/or TA support

**Enrichment:** Provided upon teacher request for entire class, small group or individual students.

Weekly pull-out math class Grades 3, 4 and 5

**After school programs at Lane:** METCO Math and Homework Club Academic

# K-5 Professional Collaborative Culture

**Grade Level Cluster Teams or Pods** - Discuss student progress and lesson planning

**Grade Level Teams** - Teacher Days with Math Discussions (around the new editions or curricula)

**Curriculum Coordinator** - Consult with individual teachers and grade level teams, analyze data of student performance, meet weekly Davis Math Support TA and Lane Title I teacher, provide pacing guides and assessments

**Teacher Days and Summer Work**





# 7th Grade: Thinking about surface area and volume

4) Discuss the surface area to volume ratio of different spheres and how it changes based on the radius. At what radius do the surface area and the volume of a sphere equal each other. Show this with calculations, algebraically and graphically.

*What a terrific graph!*  
*Outstanding*

4) The surface area to volume ratio is 3:r.

$$\frac{4\pi r^2}{\frac{4}{3}\pi r^3} = \frac{4\pi r^2}{\frac{4}{3}\pi r^3} = \frac{4}{\frac{4}{3}r} = \frac{4 \times 3}{4 \times r} = \frac{12}{4r} = \frac{3}{r}$$

This ratio changes based on what the radius is because r is a variable so it can be any number. The surface area equals the volume when the radius is 3 because the ratio is 3:3.

$$SA = \text{Volume}$$

$$4\pi r^2 = \frac{4}{3}\pi r^3$$

$$\frac{4\pi r^2}{\pi r^2} = \frac{\frac{4}{3}\pi r^3}{\pi r^2}$$

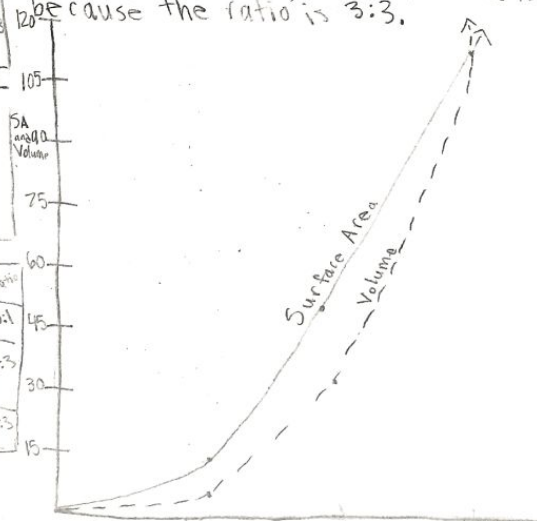
$$3 \times 4 = \frac{4}{3}r \times 3$$

$$\frac{12}{4} = \frac{4r}{4}$$

$$3 = r$$

$\pi = 3.14$

r	SA	V	Ratio
1	$4\pi$ 12.56	$\frac{4}{3}\pi$ 4.19	3:1
2	$16\pi$ 50.24	$\frac{16}{3}\pi$ 33.49	3:3
3	$36\pi$ 113.04	$\frac{36}{3}\pi$ 113.04	3:3



# Equity and Diversity: Teaching all students

## JGMS Tenacity Challenge



## MathCounts





## 8th Grade Enrollment Data

	<b>2012-2013</b> # of students	<b>2013-2014</b>	<b>2014-2015</b>	<b>2015-2016</b>
<b>Pre-Algebra</b>	56 (28%)	63 (32%)	49 (29%)	<b>26 (15%)</b>
<b>Algebra</b>	144 (72%)	134 (68%)	119 (71%)	90 (53%)
<b>Algebra IA</b>	0	0	0	54 (32%)
<b>Total</b>	200 students	197 students	168 students	170 students

# JGMS Professional Collaboration

7<sup>th</sup> grade

8<sup>th</sup> grade

9<sup>th</sup> grade

7<sup>th</sup> Grade  
Math

8<sup>th</sup> Grade Pre  
Algebra

Algebra  
College Prep

Algebra  
Honors

7<sup>th</sup> Grade  
PreAlgebra

8<sup>th</sup> Grade  
Algebra 1A

Continuing  
Alg/Geo Honors

8<sup>th</sup> Grade  
Algebra

Geometry  
Honors

Geometry  
High Honors

## 8th Pre Algebra

STEM  
Applications

Algebra  
CP

Algebra  
Honors

Algebra  
CP

Geometry  
CP

Geometry  
Honors

Geometry  
CP

Algebra II  
CP

Algebra II  
Honors

Algebra II  
CP / Business  
Math CP

Business  
Math CP

Pre-Calc,  
Statistics,  
Business  
Math CP/H

## 8th Algebra (1 or 1A)

Cont.  
Alg/Geo H

Geometry  
Honors

Geometry  
High Honors

Cont. Geo/  
Alg II H

Algebra II  
Honors

Algebra II  
High Honors

Cont. Alg II/  
Pre-Calc  
Honors

PreCalc  
Honors

PreCalc  
High Honors

**Calculus H,**  
Statistics, or  
Business Math

**Calculus  
Honors**

**Calculus AP  
AB and BC**

# BHS Coherent, Standards-based Curriculum



## Strong Professional Collaboration

# Student Centered Learning that makes kids think...

15)

Diagram showing a triangle with sides 300m, 500m, and 200m. The angle between the 300m and 500m sides is  $105^\circ$ . The angle between the 500m and 200m sides is  $106.24^\circ$ . The angle between the 300m and 200m sides is  $28.76^\circ$ . The area of the triangle is calculated as the sum of two smaller triangles.

Area 1:

$$A_1 = \frac{1}{2}(300)(200)\sin 105^\circ$$

$$A_1 = 28977.77479 \text{ m}^2$$

Area 2:

$$x^2 = 300^2 + 200^2 - 2(300)(200)\cos 105^\circ$$

$$x^2 = 150000 - 120000\cos 105^\circ$$

$$x = 401.32$$

Area 2 (using x):

$$A_2 = \frac{1}{2}(500)(401.32)\sin 106.24^\circ$$

$$A_2 = 96326.7 \text{ m}^2$$

Total Area:

$$A_{\text{tot}} = A_1 + A_2 = 165304.48 \text{ m}^2$$

Additional calculations on the right:

$$200^2 = 300^2 + 401.32^2 - 2(300)(401.32)\cos \theta$$

$$\cos \theta = \frac{211057.74}{240700}$$

$$\theta = 28.76^\circ$$

# Challenging Tasks

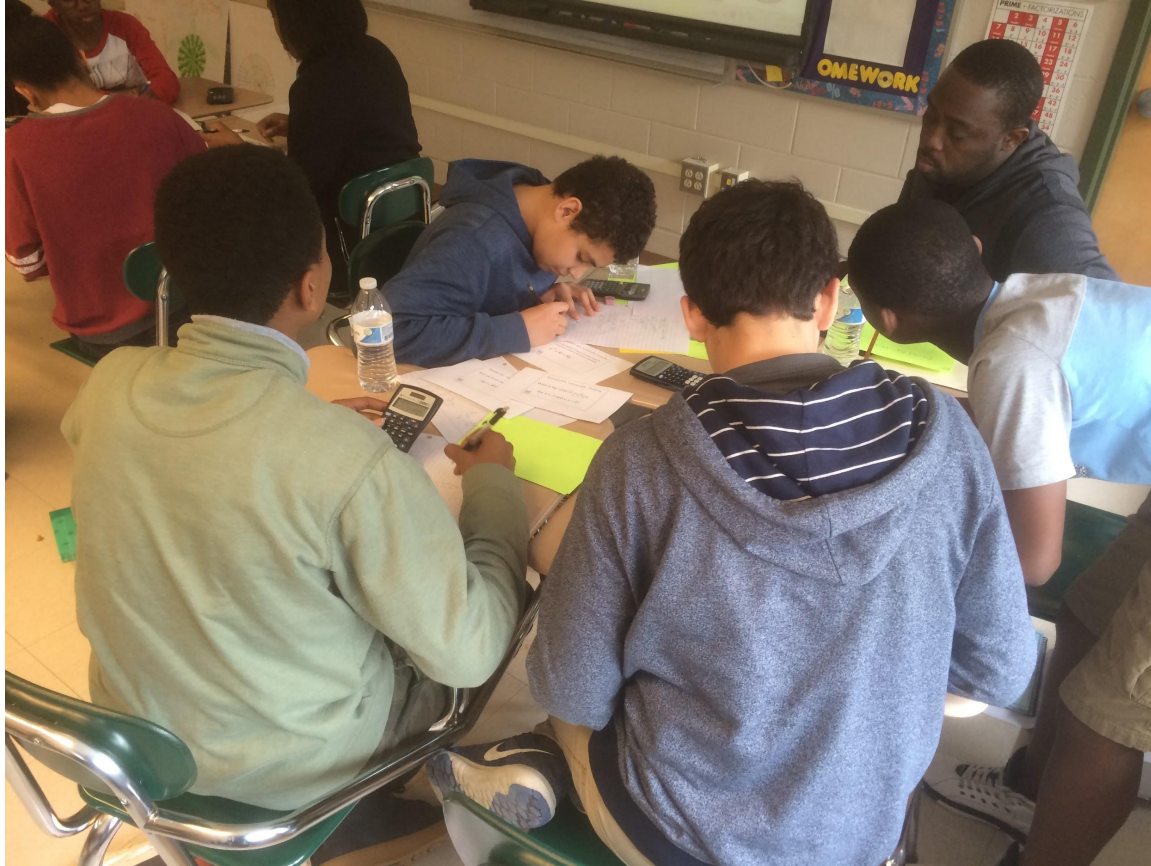




# Student Centered Learning



# Equity and Diversity: Teaching all students





# Challenges

- BHS Department Reputation
- MCAS Scores
- Support for co-teaching classes at JGMS and BHS
- Lack of Common Planning time at BHS
- Sharing classrooms at BHS, need for laptops for all
- “Continuing” Sequence of courses

# 10th Grade MCAS

	2011	2012	2013	2014	2015
<b>Advanced</b>	76%	73%	80%	76%	72%
<b>Proficient</b>	17%	20%	14%	19%	19%
<b>Needs Improvement</b>	6%	7%	3%	4%	8%
<b>Warning</b>	0%	0%	2%	1%	2%

Some columns don't add to 100% due to rounding errors.

# BHS: Looking Ahead

- Analyzing student work in PLCs and between buildings
- Co-Teaching support
- Shared collaborative workroom
- Drop in Help Center
- Adding AP Stats
- Focused MCAS support with identified populations